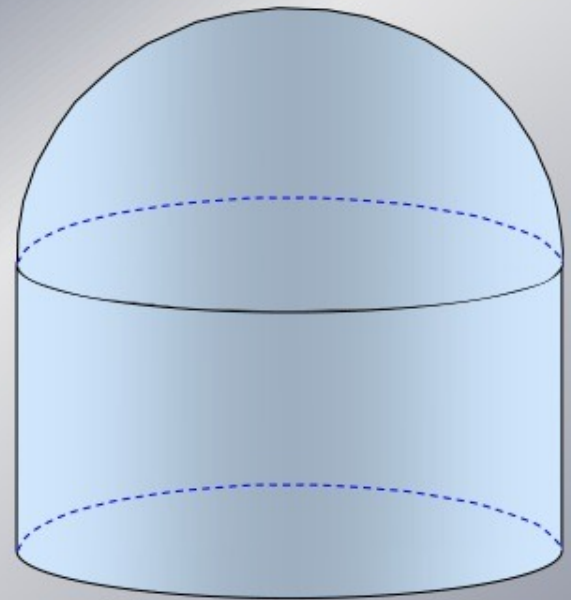
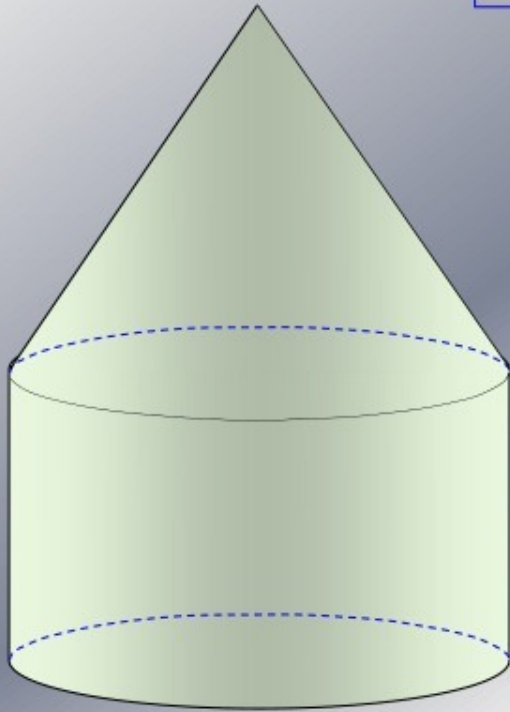


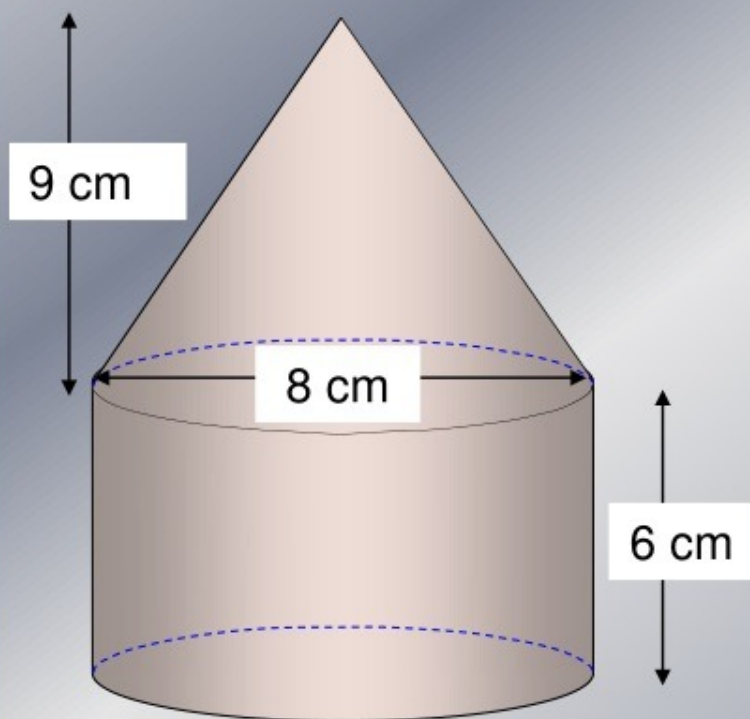
Composite Solids



Example Question 1

Composite Solids

An aeronautical engineer designs a small component part made of copper, that is to be used in the manufacturer of an aircraft. The part consists of a cone that sits on top of a cylinder as shown in the diagram below. Find the volume of the part. (Leave your answer in terms of π).



$$\begin{aligned}\text{Volume of cone} &= \frac{1}{3} \pi r^2 h \\ &= \frac{1}{3} \times \pi \times 4^2 \times 9 \\ &= 48 \pi \text{ cm}^3\end{aligned}$$

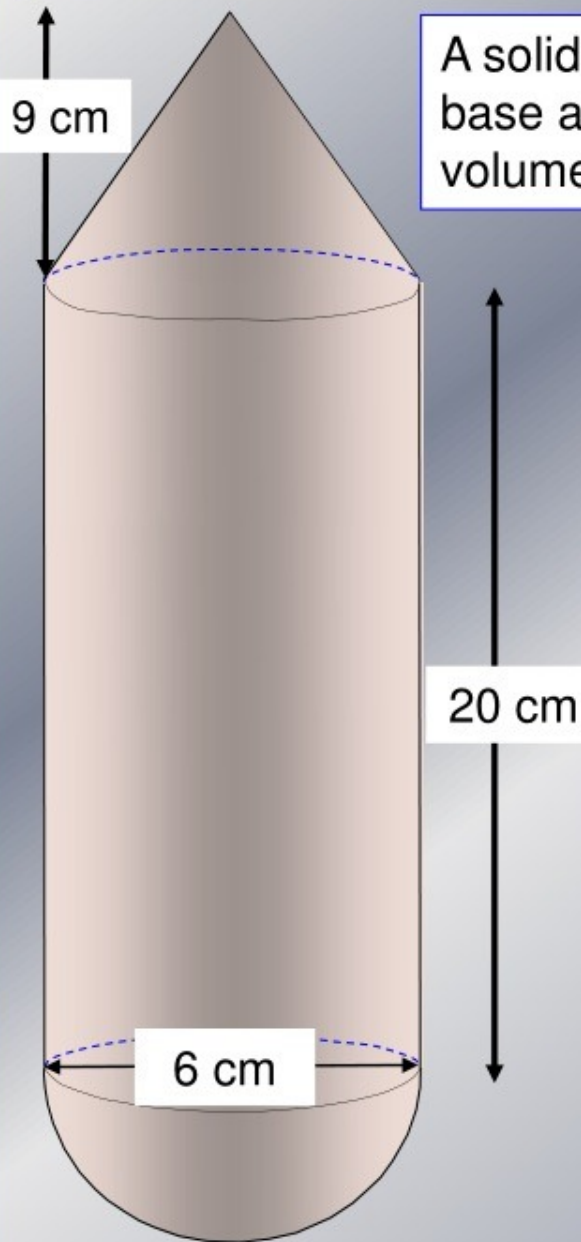
$$\begin{aligned}\text{Volume of cylinder} &= \pi r^2 h \\ &= \pi \times 4^2 \times 6 \\ &= 96 \pi \text{ cm}^3\end{aligned}$$

$$\text{Total volume} = 48 \pi + 96 \pi = \underline{144 \pi \text{ cm}^3}$$

Question 4

Composite Solids

A solid shape is composed of a cylinder with a hemi-spherical base and a conical top as shown in the diagram. Calculate the volume of the shape. (answer to 2 sig fig)



$$\begin{aligned}\text{Volume of cone} &= \frac{1}{3} \times \pi r^2 h \\ &= \frac{1}{3} \times \pi \times 3^2 \times 9 \\ &= 27\pi \text{ cm}^3\end{aligned}$$

$$\begin{aligned}\text{Volume of cylinder} &= \pi r^2 h \\ &= \pi \times 3^2 \times 20 \\ &= 180\pi \text{ cm}^3\end{aligned}$$

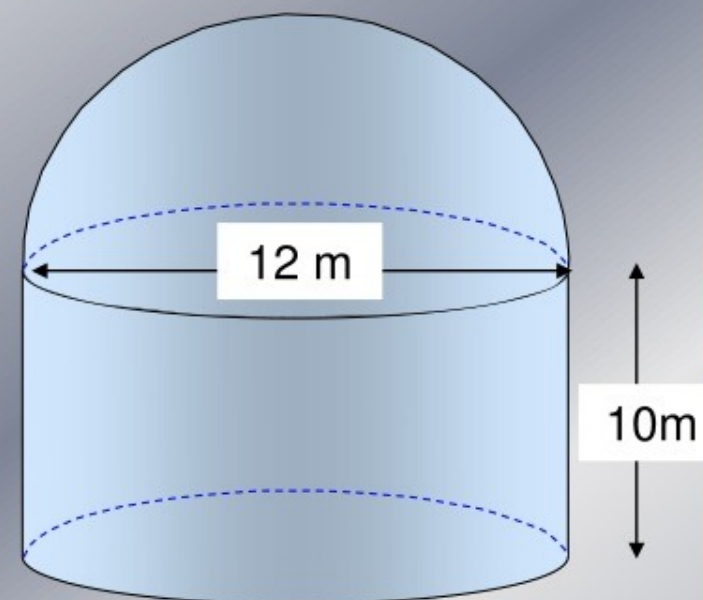
$$\begin{aligned}\text{Volume of hemi-sphere} &= \frac{2}{3} \pi r^3 \\ &= \frac{2}{3} \times \pi \times 3^3 \\ &= 18\pi \text{ cm}^3\end{aligned}$$

$$\begin{aligned}\text{Total volume} &= 27\pi + 180\pi + 18\pi = 225\pi \text{ cm}^3 \\ &= \underline{710 \text{ cm}^3}\end{aligned}$$

Question 3

Composite Solids

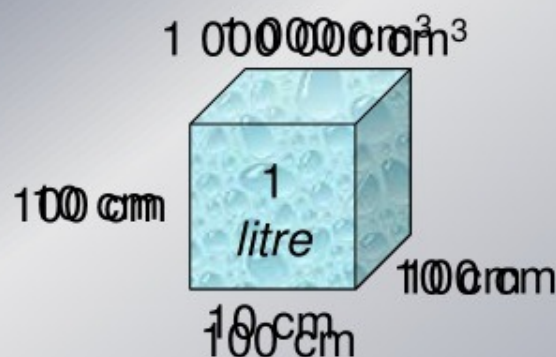
The diagram below shows a design for a water tank. The water tank consists of a cylinder capped with a hemi-spherical dome. Find the capacity of the water tank. (Give your answer in litres to 3 sig fig).



$$\begin{aligned}\text{Capacity of hemi-sphere} &= \frac{2}{3} \pi r^3 \\ &= \frac{2}{3} \times \pi \times 6^3 \\ &= 144 \pi \text{ m}^3\end{aligned}$$

$$\begin{aligned}\text{Capacity of cylinder} &= \pi r^2 h \\ &= \pi \times 6^2 \times 10 \\ &= 360 \pi \text{ m}^3\end{aligned}$$

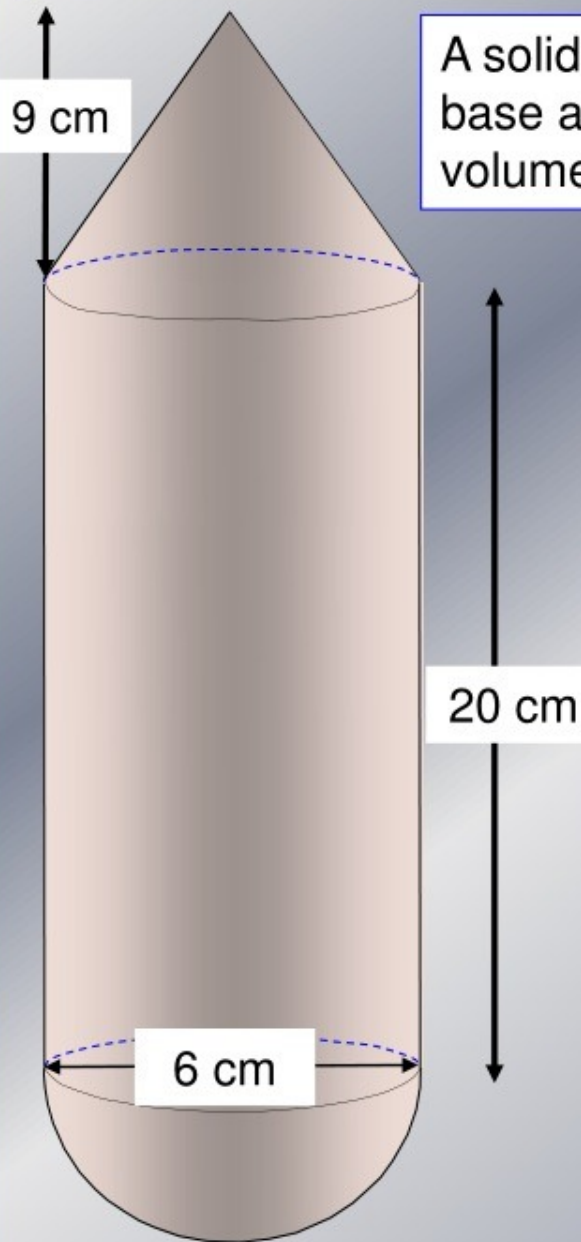
$$\begin{aligned}\text{Total capacity} &= 144 \pi + 360 \pi = 504 \pi \text{ m}^3 \\ &= 504\,000\,000 \pi \text{ cm}^3 \\ &= 504\,000 \pi \text{ litres} \\ &= \underline{1\,580\,000 \text{ litres}} \text{ (3 sig fig)}\end{aligned}$$



Question 4

Composite Solids

A solid shape is composed of a cylinder with a hemi-spherical base and a conical top as shown in the diagram. Calculate the volume of the shape. (answer to 2 sig fig)



$$\begin{aligned}\text{Volume of cone} &= \frac{1}{3} \times \pi r^2 h \\ &= \frac{1}{3} \times \pi \times 3^2 \times 9 \\ &= 27\pi \text{ cm}^3\end{aligned}$$

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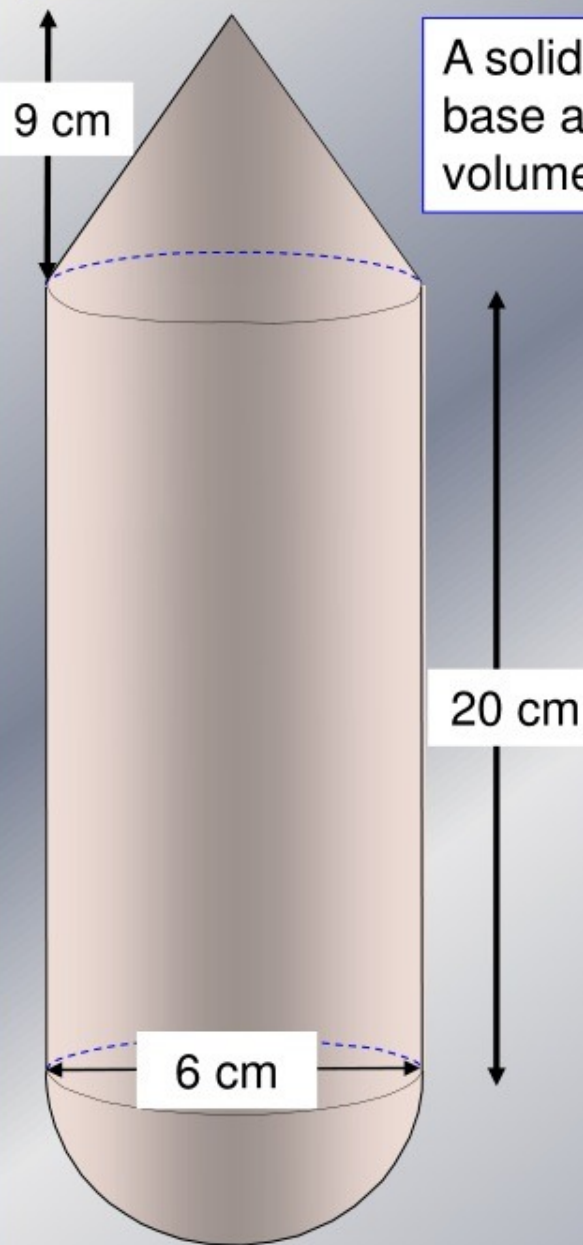
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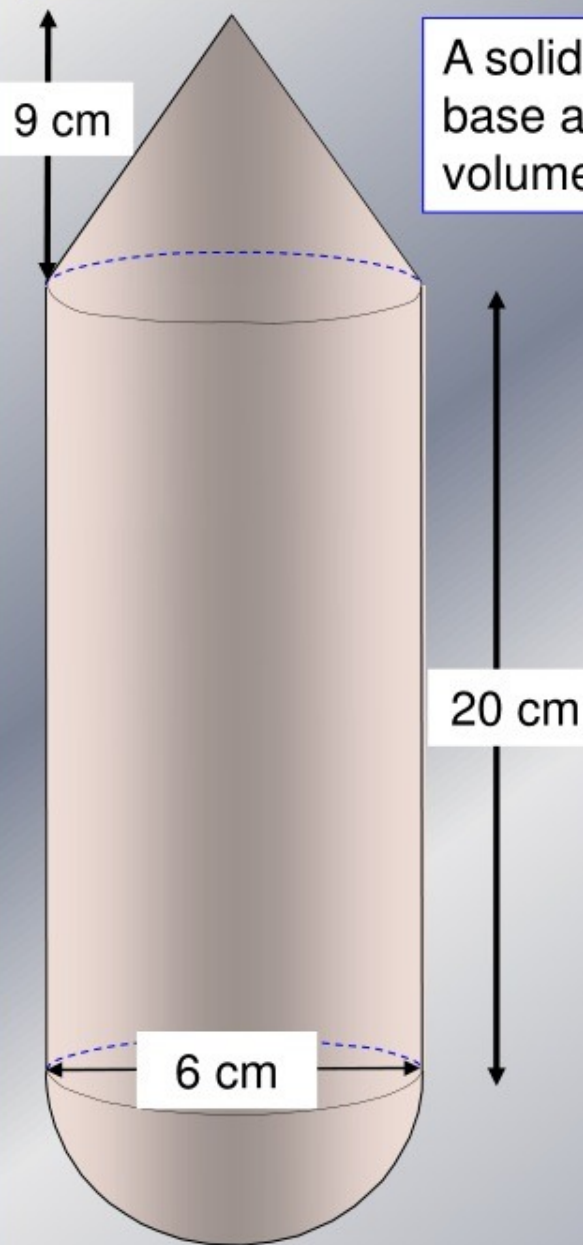
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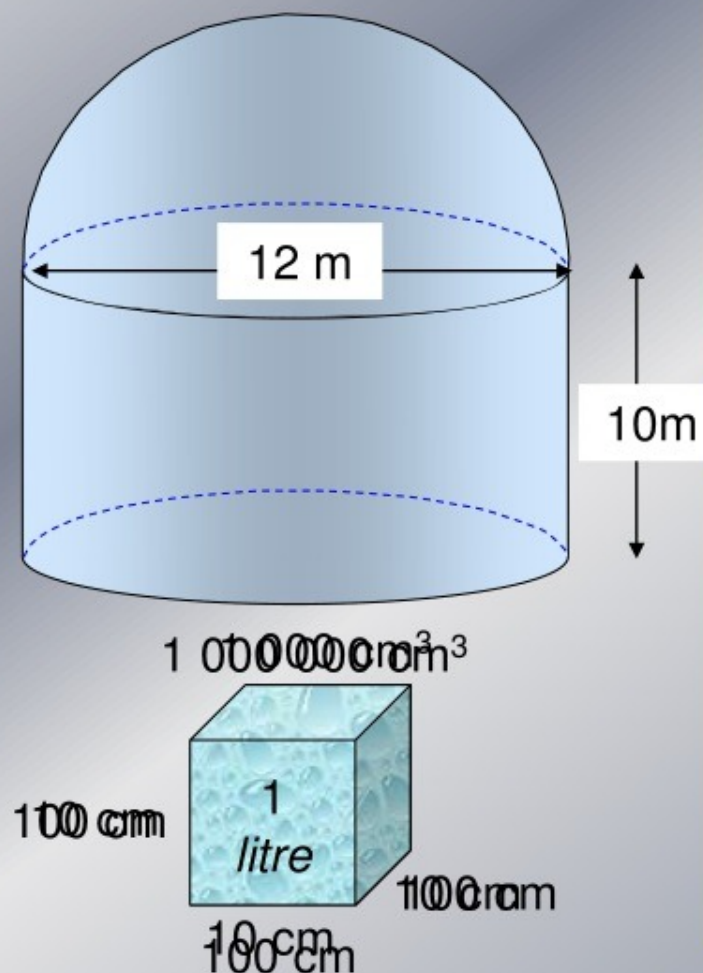
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Question 3

Composite Solids

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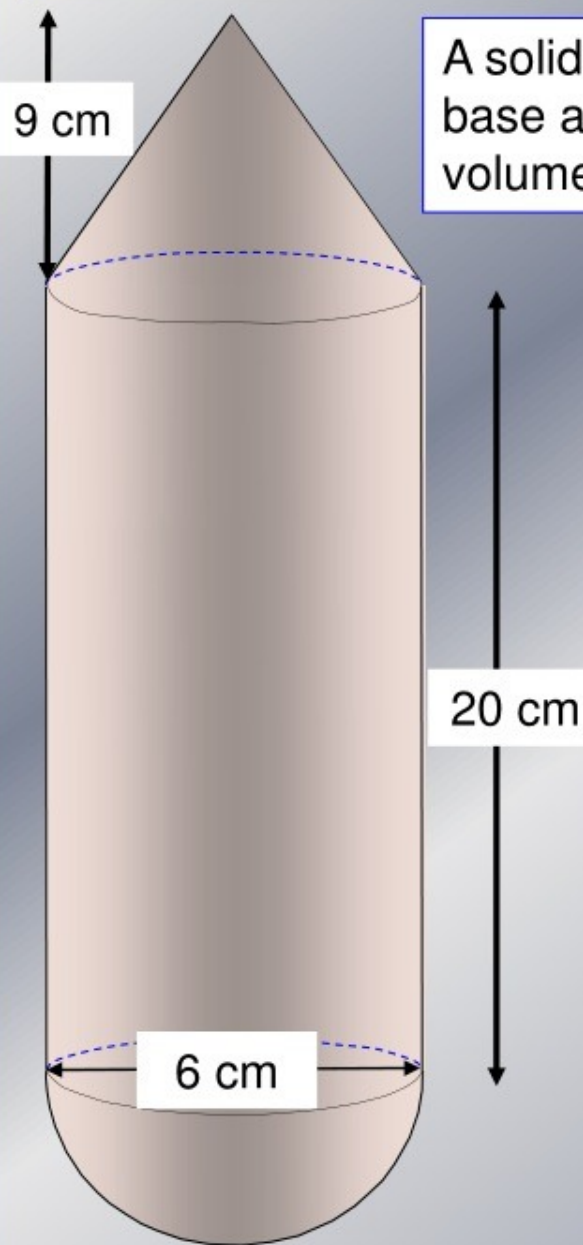
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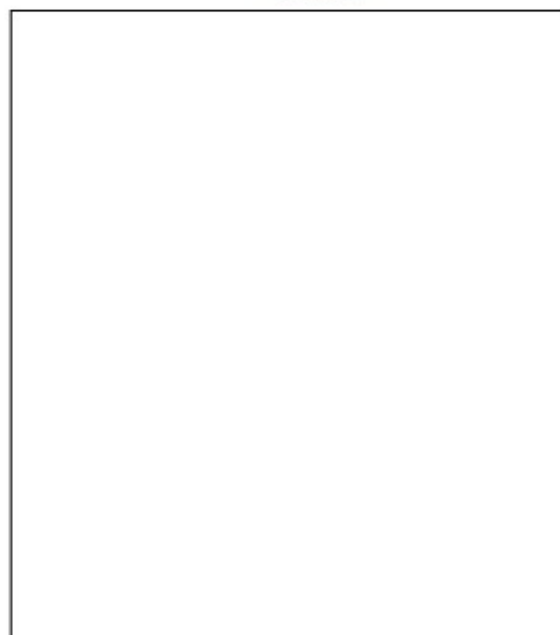
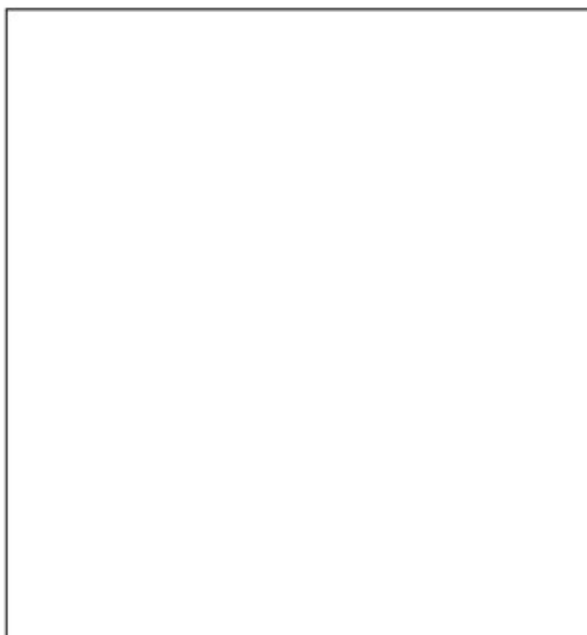
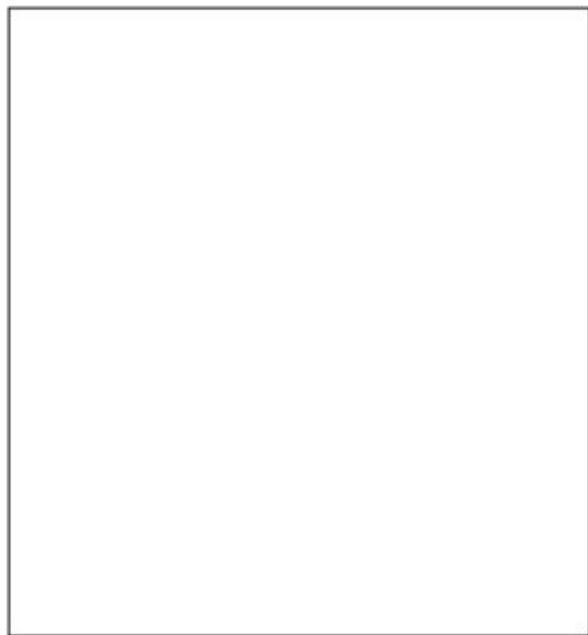
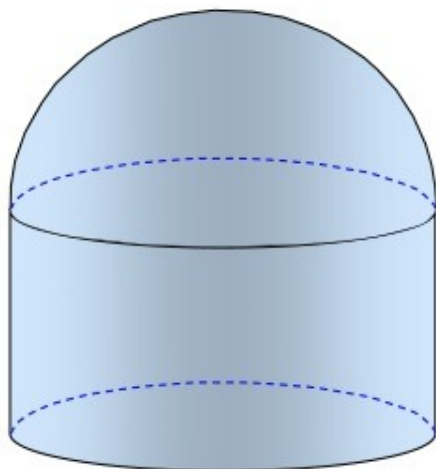
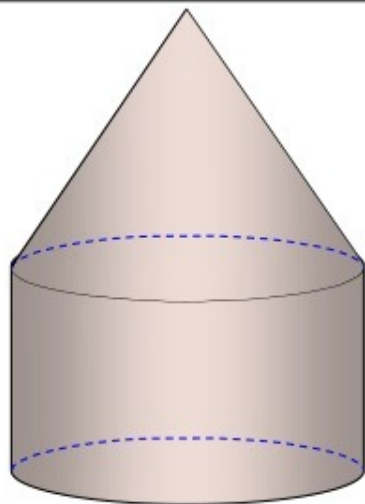
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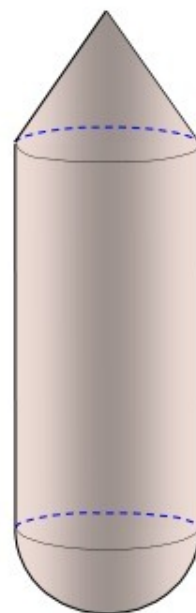
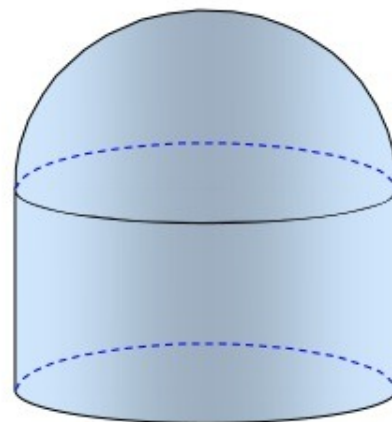
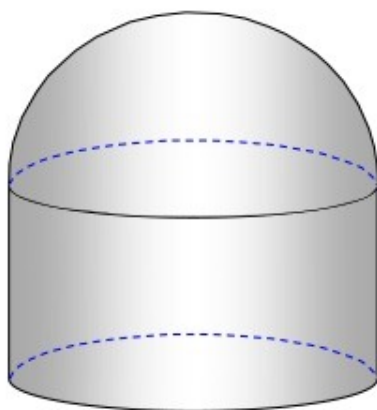
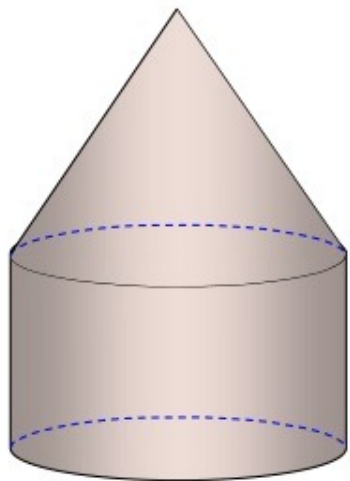
Example Questions

Surface Area



Questions

Volume/Capacity



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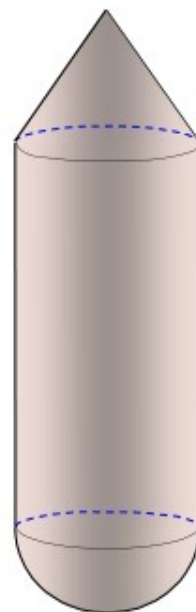
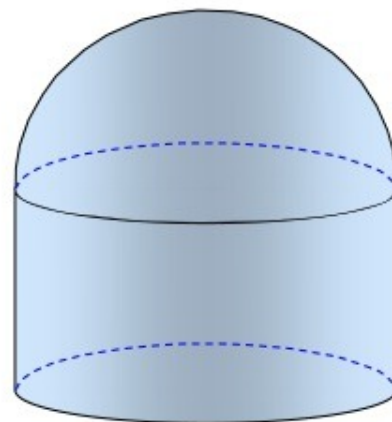
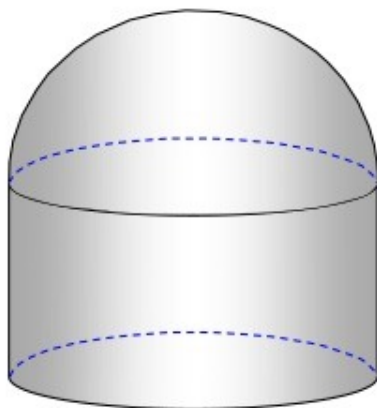
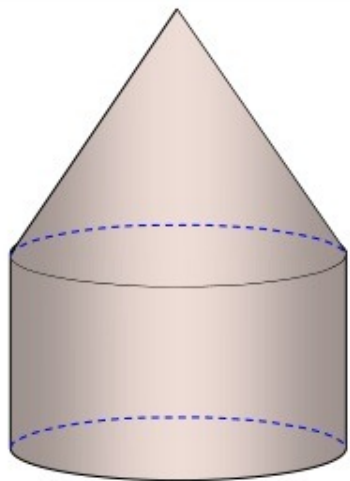
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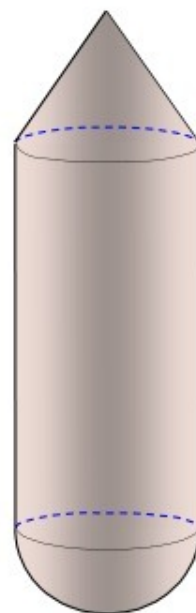
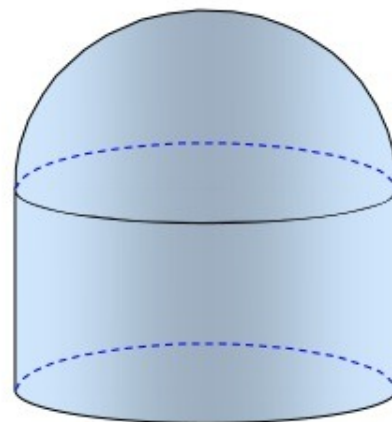
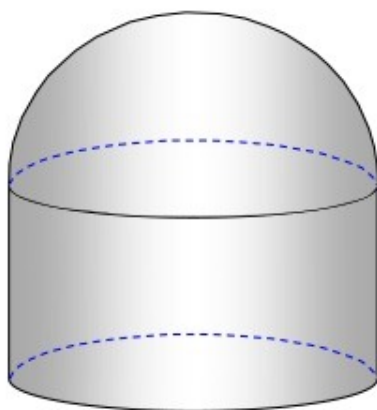
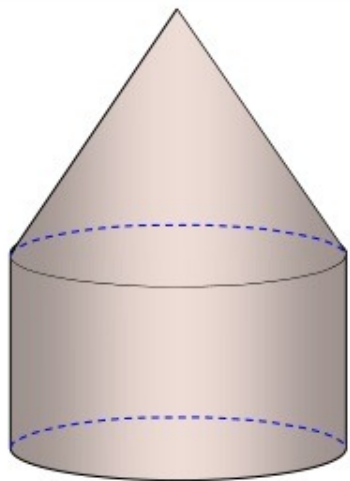
Example Questions

Volume/Capacity



Questions

Volume/Capacity



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